## Banach Lie-Poisson spaces related to $W^*$ -algebras

Anatol Odzijewicz Institute of Mathematics, University of Byalimstok Byalimstok, Poland

## Abstract

We introduce the notion of Banach Lie-Poisson space as a natural generalization of the finite dimensional linear Poisson structure. Some crucial theorems concerning the category of these objects will be presented. We show that the preduals of  $W^*$ -algebras form a subcategory in the category of Banach Lie-Poisson spaces. Examples and applications in the quantum physics and in the theory of integrable systems will be presented.